

$$|Tf|^2 = \int_{-\pi}^{\pi} |Tf(x)|^2 dx \leq \int_{-\pi}^{\pi} \left(\sup_n |\lambda_n| \right)^2 |f(x)|^2 dx = \left(\sup_n |\lambda_n| \right)^2 |f|^2.$$