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$$H(e^{j\omega}) = \mathcal{F}(h_1(n) + h_2(n))$$

$$\mathcal{F}(h_1(n)) = \sum_{n=-\infty}^{+\infty} \left(\frac{1}{3}\right)^n u(n) e^{-j\omega n}$$

$$= \frac{1}{1 - \frac{1}{3} e^{-j\omega}}$$

$$H(e^{j\omega}) - \mathcal{F}(h_1(n)) = -1 + \frac{\frac{1}{3}}{e^{j\omega} - \frac{1}{3}} + \frac{-\frac{1}{2}}{e^{j\omega} - \frac{1}{4}} = \left(1 + \frac{\frac{1}{3}}{e^{j\omega} - \frac{1}{3}}\right)$$

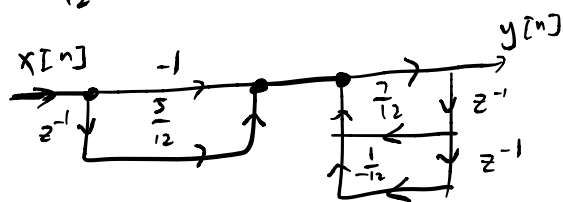
$$= -2 + \frac{-\frac{1}{2}}{e^{j\omega} - \frac{1}{4}}$$

$$\text{so. } h_2(n) = -2 \mathcal{F}^{-1}\left(\frac{\frac{1}{4}}{e^{j\omega} - \frac{1}{4}} + 1\right)$$

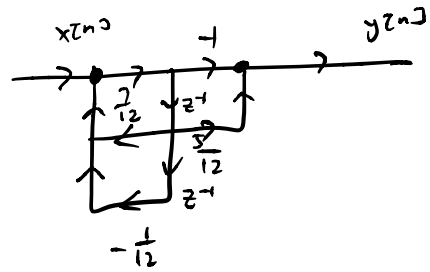
$$= -2 \left(\frac{1}{4}\right)^n u(n)$$

$$(2) \quad H(z) = \frac{-1 + \frac{5}{12} z^{-1}}{1 - \frac{7}{12} z^{-1} + \frac{1}{12} z^{-2}}$$

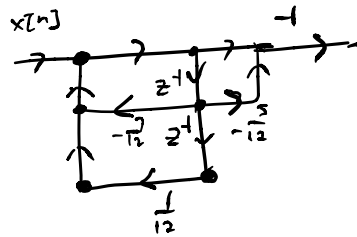
Direct Form I:



Direct Form II:



Cascade Form:



PARALLEL Form.

