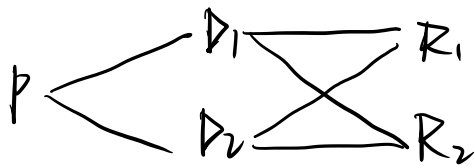


Q1. (a)



Let route (P, D_1, R_1) be a

route (P, D_1, R_2) be b

route (P, D_2, R_1) be c

route (P, D_2, R_2) be d

then objective function (minimize total shipping costs)

$$\text{Min } 8a + 13b + 9c + 11d$$

subject to $a + b + c + d = 1000$ (production capacity)

$$\left. \begin{array}{l} a + b \leq 400 \\ c + d \leq 700 \end{array} \right\} \text{capacity constraints for } D_1 \text{ \& } D_2$$

$$\left. \begin{array}{l} a + c = 750 \\ b + d = 250 \end{array} \right\} \text{demand constraints}$$

$$\left. \begin{array}{l} 0 \leq a + b \leq 550 \\ 0 \leq c + d \leq 650 \\ 0 \leq a \leq 350 \\ 0 \leq b \leq 250 \\ 0 \leq c \leq 550 \\ 0 \leq d \leq 450 \end{array} \right\} \text{shipping quantity constraints}$$

(b) change production capacity constraint from 1000 to 800

$$a + b + c + d = 800$$

New info needed: How the 800 units allocate between R_1 and R_2 .

Q3. (1) Let unit of production for Model A be x ,
unit of production for Model B be y ,

Objective function (maximize unit contribution)

$$\text{Max } 70x + 40y$$

Subject to $0 \leq x \leq 2000$ (max demand)
 $0 \leq y \leq 4000$

$$0 \leq 1.5x \leq 2500 \quad (\text{production capacity})$$
$$0 \leq y \leq 4500$$

(2) only change in production capacity constraint:

$$0 \leq 1.6x + 1.1y \leq 7000$$

(3) Let unit of dedicated production for Model A be m ,
unit of flexible production for Model A be n ,
unit of dedicated production for Model B be p ,
unit of flexible production for Model B be q ,

Objective function (maximize unit contribution)

$$\text{Max } 70(m+n) + 40(p+q)$$

Subject to $0 \leq m+n \leq 2000$ (max demand)

$$0 \leq p+q \leq 4000$$

$$0 \leq 1.5m \leq 900$$

$$0 \leq p \leq 1100 \quad (\text{production capacity})$$

$$0 \leq 1.6n + 1.1q \leq 5000$$

$$(4) \text{ Max } 70(m+n) + 40(p+q) - 7000 \mathbb{1}_n - 5000 \mathbb{1}_q$$

$$\text{Subject to } 0 \leq m+n \leq 2000 \quad (\text{max demand})$$

$$0 \leq p+q \leq 4000$$

$$0 \leq 1.5m \leq 900$$

$$0 \leq p \leq 1100 \quad (\text{production capacity})$$

$$0 \leq 1.6n + 1.1q + 100 \mathbb{1}_n + 75 \mathbb{1}_q \leq 5000$$

$$\text{where } \mathbb{1}_n = \begin{cases} 1, & \text{if } n > 0 \\ 0, & \text{if } n = 0 \end{cases}$$

