

1. Let $X_{(n)} = \min \{X_i\}_{i=1}^n$.

then

$$F_{X_{(n)}}(x) = P(X_{(n)} \leq x)$$

$$= 1 - P(X_{(n)} > x)$$

$$= 1 - P(\min\{X_i\}_{i=1}^n > x)$$

$$= 1 - P(X_1 > x, X_2 > x, \dots, X_n > x)$$

$$= 1 - P(X_1 > x)$$

$$= 1 - (1 - F_X(x))^n$$

2. $F_X(x) = \frac{x}{\theta}$

$$F_{X(n)}(x) = (F_X(x))^n = \left(\frac{x}{\theta}\right)^n, \quad 0 \leq x \leq \theta$$

3.

$$F_{X(n)}(x) = 1 - (1 - F_X(x))^n$$

$$= 1 - \left(1 - \frac{x}{\theta}\right)^n$$

$$= 1 - \left(\frac{\theta - x}{\theta}\right)^n, \quad 0 \leq x \leq \theta$$