

7.

$$1. X, Y \sim U(0, 1) \quad f_{X,Y} = f_X(x) f_Y(y) = \begin{cases} 1, & 0 \leq x, y \leq 1 \\ 0, & \text{其他} \end{cases}$$

$$\text{当 } 0 \leq z < 1 \text{ 时, } f_z(z) = \int_0^z dx = z.$$

$$\text{当 } 1 \leq z < 2 \text{ 时, } f_z(z) = \int_{z-1}^1 dx = 2 - z$$

$$\therefore f_z(z) = \begin{cases} z, & 0 \leq z < 1 \\ 2 - z, & 1 \leq z < 2 \\ 0, & \text{其他} \end{cases}$$

$$2. X, Y \sim \text{Exp}(1)$$

$$f_X(x) = e^{-x}, \quad x > 0$$

$$\text{当 } z > 0.$$

$$f_z(z) = \int_0^z e^{-x} \cdot e^{-z+x} dx = z e^{-z}$$

$$\therefore f_z(z) = \begin{cases} z e^{-z}, & z > 0 \\ 0, & \text{其他} \end{cases}$$