

1° Let $\bar{X}_n$ denote the sample mean of the annual salaries.

then the confidence interval takes the form

$$[\bar{X}_n - z_{\alpha/2} \text{sd}(\bar{X}_n), \bar{X}_n + z_{\alpha/2} \text{sd}(\bar{X}_n)],$$

which is

$$[\bar{X}_n - z_{0.005} \frac{15000}{\sqrt{n}}, \bar{X}_n + z_{0.005} \frac{15000}{\sqrt{n}}]$$

2^o

The interval length is

$$2 \cdot Z_{0.005} \frac{15000}{\sqrt{n}} \leq 5000$$

$$2 \cdot 2.57 \cdot \frac{15000}{\sqrt{n}} \leq 5000$$

$$\sqrt{n} \geq 15.42$$

$$n \geq 237.78$$

So the minimum value of n

is $n = 238$.

$$3^{\circ} \quad n = 50$$

$$\bar{X}_n = 52000$$

The one-side confidence interval is

$$(-\infty, \bar{X}_n + \frac{6}{\sqrt{n}} \cdot Z_{0.01}]$$

Thus

$$b = \bar{X}_n + \frac{6}{\sqrt{n}} Z_{0.01}$$

$$= 52000 + \frac{15000}{\sqrt{50}} \cdot 2.33$$

$$= 56942.68$$

Thus the one side confidence interval is

$$(-\infty, 56942.68]$$